MIT Physics PhD Core Requirements Syllabus

Classical Mechanics:

- 1. Newton's laws for systems of particles (momentum, energy, center of mass, angular momentum, friction, solutions for motion, relativistic mechanics)
- 2. Lagrangian and Hamiltonian formulations of mechanics (calculus of variations, Lagrangian and Hamiltonian equations of motion, Legendre transformation)
- 3. Symmetry and Noether's theorem (cyclic coordinates, conservation laws)
- 4. Constraints (constraints to surfaces by elimination of variables, use of Lagrange multipliers, generalized forces such as forces of constraint)
- 5. Orbits and Scattering (motion in a central field, reduced mass, Kepler's problem, Rutherford scattering)
- 6. Vibrations and Oscillations (normal modes, simultaneous diagonalization of kinetic and potential energy matrices, superposition principle)
- 7. Canonical transformations (generating functions, Poisson brackets, Liouville's theorem)
- 8. Rigid body motion (moment of inertia tensor, Euler equations, centrifugal and Coriolis fictitious forces, precession and nutation)
- 9. Basics of fluid mechanics (continuity equation, ideal fluids, shear viscosity, Euler and Navier-Stokes equations, steady flows, Reynolds number)

References for these topics:

- Latex lecture notes for 8.309, by lain Stewart (covers all topics in suitable depth except for A and E): <u>Stewart-Classical-Mechanics-III</u>
- *Classical Mechanics,* by Goldstein, Poole, Safko (covers all qualifying exam topics except for fluid mechanics)

Other references which may be useful include *Classical Dynamics* by Thornton and Marion (good reference at slightly lower level than Goldstein); *Mechanics* by Symon (good reference for its chapter on perfect fluids); Landau and Lifshitz volume 1 (for general mechanics) and volume 6 (for viscous fluids); Fluid Mechanics by Smits (useful for fluid problems); *Classical Dynamics: a Contemporary Approach* by Jose and Saletan (a relatively mathematical approach that also includes more modern topics and hydrodynamics)

Electromagnetism

- 1. Basics of EM
 - 1.1 Charges, currents
 - 1.2 Maxwell's Equations in vacuum
 - 1.3 Scalar and Vector Potentials

1.4 Fields in materials (polarizability, magnetization, macroscopic fields, linear materials, Ohm's law)

- 1.5 Boundary Conditions at Interfaces
- 1.6 Electrostatic and magnetostatic limits
- 1.7 Energy in electric fields and magnetic fields
- 2. Boundary Value Problems
 - 2.1 Method of images
 - 2.2 Separation of variables: cartesian, spherical, cylindrical coordinates
 - 2.3 Green Function methods
 - 2.4 Multipole methods
 - 2.5 Boundary value problems in materials
- 3. Waves and wave guides
 - 3.1 Electromagnetic waves in vacuum
 - 3.2 Polarization
 - 3.3 Poynting vector and intensity
 - 3.3 Electromagnetic waves in materials
 - 3.4 Reflection/refraction from an interface
 - 3.5 Propagation in a wave guide
- 4. Radiation
 - 4.1 Lienard-Wiechert solution of Maxwell's equations in Lorenz gauge
 - 4.2 Far-field and non-relativistic approximations
 - 4.3 Electric and magnetic dipole radiation
 - 4.4 Multipole radiation
- 5. Scattering and diffraction
 - 5.1 Scattering of EM waves
 - 5.2 Long wavelength
 - 5.3 Short wavelength
 - 5.4 Diffraction (scalar case)
- 6. Relativistic electrodynamics
 - 6.1 Covariant form of Maxwell's equations
 - 6.2 Lagrangian formulation of the EM field
 - 6.3 Energy-momentum tensor and conservation laws
 - 6.3 Relativistic motion of charged particles in uniform E and B fields

- 6.4 Solution of covariant wave equation
- 7. Radiation by relativistic charges
 - 7.1 Radiation by an accelerated point charge
 - 7.2 Thomson scattering
 - 7.3 Bremsstrahlung, synchrotron radiation

The level here is intermediate between *Introduction to Electrodynamics* by Griffiths and *Classical Electrodynamics* by Jackson. Topics 1), 3), 4), and 6) are mostly Griffiths material, while topics 2), 5), and 7) are mostly Jackson. Other useful sources are *Modern Electrodynamics* by Zangwill, Likharev's <u>notes</u>, volume 2 of the Feynman lectures, and Landau/Lifschitz volume 2.

Statistical Mechanics

- 1. Microcanonical ensemble, entropy, temperature. Examples from ideal gas, discrete systems (spins, vacancies, etc.)
- 2. Thermodynamics from statistical mechanics, temperature, heat, work
- 3. Canonical and grand canonical ensembles; classical ideal gas
- 4. Kinetic theory of gases (Liouville's theorem, linearized Boltzman equation, H-theorem, approach to equilibrium)
- 5. Quantum statistics, density matrices, fermions and bosons
- 6. Ideal gas of non-interacting fermions
- 7. Ideal gas of non-interacting bosons
- 8. Phase diagram of an Ising magnet (exact results in one-dimension, mean-field approach in higher dimensions)
- 9. Phase diagram of water; latent heat
- 10. Van der Waals equation, critical point, Maxwell construction
- 11. Random walks, Brownian motion, diffusion, Einstein relation

References:

- Statistical Physics of Particles, by Kardar (textbook, videos, and lecture notes)
- Statistical Mechanics: Entropy, Order Parameters, and Complexity, by Sethna
- Material for topic 11 is available (videos and notes) on the web-course "Mathematical methods for aspiring physicists," developed by Kardar and Detmold.

Quantum Mechanics

- 1. Formalism of quantum mechanics:
 - 1.1. Hilbert space, operators, the measurement postulate
 - 1.2. The uncertainty principle
 - 1.3. Pictures: Schrödinger, Heisenberg, Interaction
- 2. Quantum mechanics of particles in a potential with and without spin
 - 2.1. Square well potential
 - 2.2. Quantum harmonic oscillator via Schrödinger equation as well as algebraically via creation/annihilation operators, coherent and squeezed states
 - 2.3. Orbital angular momentum
 - 2.4. Central potentials
 - 2.5. Hydrogen atom (including fine structure, hyperfine structure and Zeeman effect)
- 3. Symmetries

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- 3.1. Continuous symmetries and conservation laws
- 3.2. Time and space translations, rotations
- 3.3. Spin, representations of SU(2)
- 3.4. Time reversal and parity
- 3.5. Degeneracies
- 3.6. Addition of angular momentum
- Particle motion under the influence of electromagnetic fields
- 4.1. Gauge invariance
- 4.2. Landau levels
- 4.3. Aharonov-Bohm effect
- 5. Approximate methods
 - 6. Variational principle
 - 7. WKB approximation and the classical limit
 - 7.1. Time-independent perturbation theory (including degenerate perturbation theory)
 - 7.2. Time-dependent perturbation theory, Fermi's Golden rule
 - 7.3. Interaction of atoms with classical EM fields, Einstein A and B coefficients, selection rules
 - 7.4. Adiabatic approximation, Berry's phase
- 7.5. Quantum mechanics of identical particles
 - 7.6. Bosons and fermions,
 - 7.7. Exclusion principle,
 - 7.8. Permutation symmetry and symmetrization
 - 7.9. Exchange interactions
 - 8. Entanglement
 - 8.1. Density matrices
 - 8.2. Von Neumann entropy
 - 8.3. Bell inequality
 - 9. Scattering theory
 - 9.1. One-dimensional scattering

- 9.2. Lippmann Schwinger Equation, Born and Eikonal approximations, Optical theorem
- 9.3. Scattering off of a central potential in three dimensions
- 9.4. Partial waves decomposition
- 9.5. Low energy scattering, bound states, resonances

References: The level for these topics should be roughly that of the textbook *Modern Quantum Mechanics* by J. J. Sakurai. The books by Shankar and Cohen-Tannoudji are also recommended as additional resources. Weinberg's book *Lectures on Quantum Mechanics* and volume 3 of Landau/Lifshitz are excellent as well, but are at a somewhat higher level.